

Numerical models for nuclear reactor physics

Towards a common framework

From GT11 prospective's contribution :

LPSC - Grenoble

A. Bidaud, A. Billebaud, N. Capellan, S. Chabod, V.Ghetta, A. Nuttin, P. Rubiolo

LPC – Caen

J. –L. Lecouey, F.-R. Lecolley, N. Marie

SUBATECH - Nantes

L. Giot, N. Thiollière

IJC Lab - Orsay

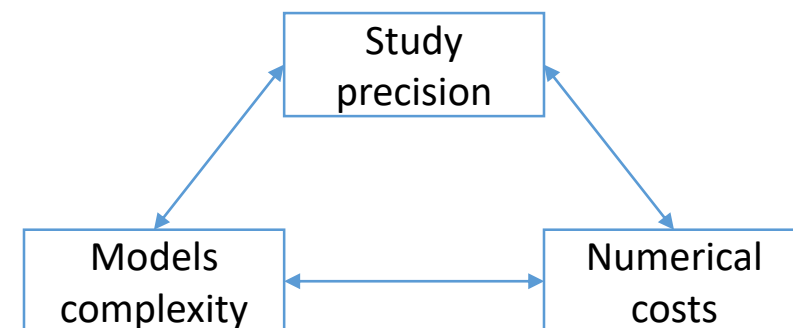
X. Doligez, M.Ernoult

- Research motivated for exploring nuclear systems potentialities for future nuclear energy (*wastes production and natural resource consumption*)
 - ~1996 first recycling studies (ADS & MSR)
 - ~2003 Beginning of MURE (MCNP Utility for Reactor Evolution)
 - Since then numerous studies involving diverse systems (CANDU, REP, RNR) – comparison between thorium and uranium fuel cycles

Pros and cons of different reactor and fuel technologies
Building a know-how in reactor modeling
Fuel the societal debate in the frame of the French law (Loi “Bataille” – 1991)

- Numerous systems studied as a way to explore reactor model options.
 - Continuous improvement of modeling tools since 2003
- **Slow evolution towards the tough spots in reactor modeling – more fundamental positioning on neutron behavior in critical media**

- IN2P3 research actions : twin track approach
 - 1. Study of systems of interest** (for the French fleet in the short term : SMR and EPR)
« cycle » and « transient » studies
 - 2. Control and reduction of uncertainties → Modeling effort**
Numerical biases, Nuclear Data, Operational data,...



- Boltzmann's equation
 - Principle and numerical difficulties
 - A two level calculation scheme for thermal neutron systems
 - Different limitations and improvement propositions
 - Nuclear data uncertainties

- Coupled calculations
 - Fuel evolution
 - Reactor models for fuel cycle simulations
 - Thermal-hydraulics coupling
 - Uncertainty propagation

- Towards a common numerical framework to gather all models
 - Interest and challenges
 - Some key points
 - As a first step : the OSCAR project

Criticality calculations : solving Boltzmann's equation

- Boltzmann's equation : looking for $\psi(\vec{r}, \hat{\Omega}, E, t)$

$$\frac{1}{v} \frac{d\psi}{dt} = -\hat{\Omega} \cdot \nabla \psi - \Sigma_{tot} \psi + \int_{E'=0}^{\infty} \int_{4\pi} \Sigma_S(E' \rightarrow E, \hat{\Omega}' \rightarrow \hat{\Omega}) \psi dE' d\hat{\Omega}' + \frac{\chi}{4\pi} \int_{E'=0}^{\infty} \int_{4\pi} v \Sigma_f \psi dE' d\hat{\Omega}' + S$$

→ Temporal variation = - Disappearance by leakage and by collision + Production by transport, fission and external sources

- k_{eff} definition for the stationary equation : $M\phi = \frac{1}{k_{eff}} F\phi$ Transient studies often consider criticality → $\Phi(\vec{r}, E, t, \dots) = N(t) \cdot \phi(\vec{r}, E, \dots)$

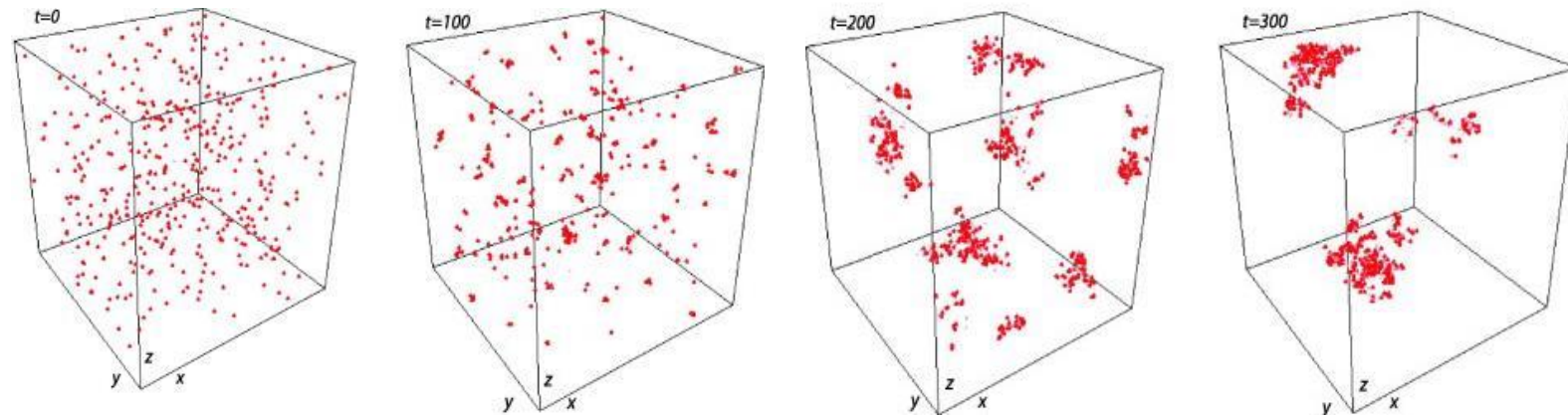
- Deterministic methods

- Energy, space and angle binning
- Impossible to compute on a full scale reactor

- Monte-Carlo methods

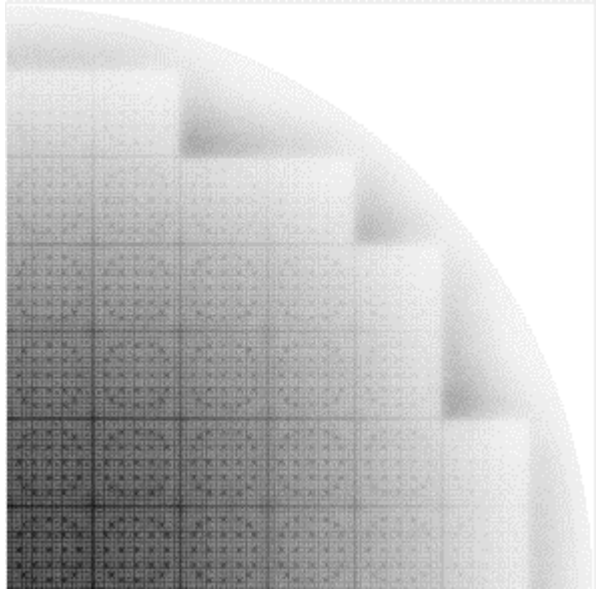
- Simulation of a great number of neutron history
- Story begins at the end of a previous one
- Source convergence issues (for thermal reactors)

E. Dumonteil, F. Malvagi, A. Zoia et al., Annals of Nuclear Energy, vol. 64, p. 612-618, 2014



Solving the neutron transport equation is "impossible" on large reactor with a thermal spectrum

Solving Boltzmann's equation : a two step algorithm for thermal reactors



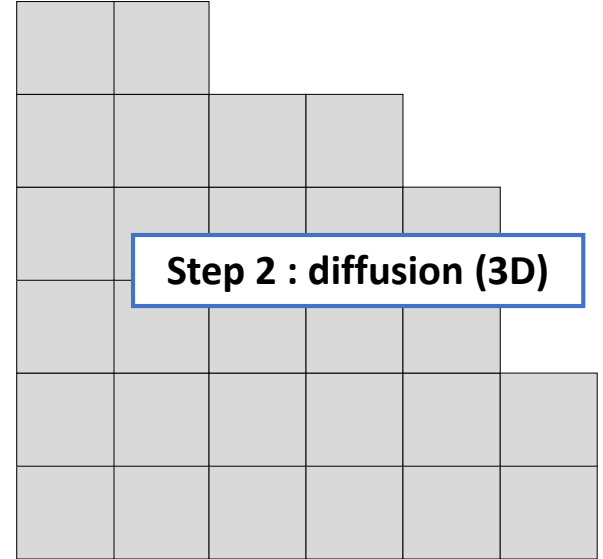
Mean behavior of each assembly :

- 2 energy groups
- Homogenized geometry
- No more angle variable (Fick's law)

Extreme simplification of the neutron balance

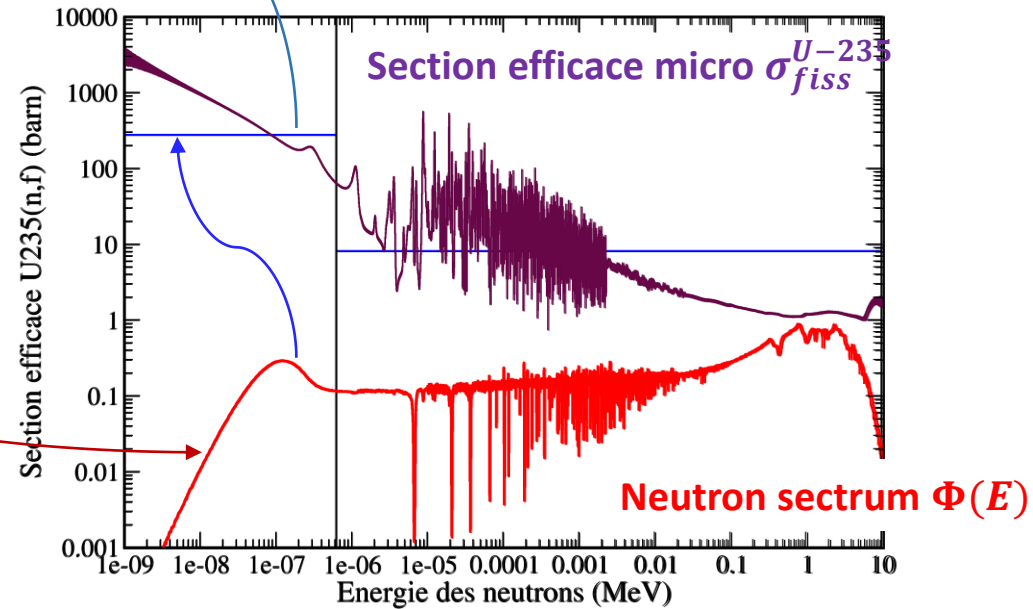
$$\Delta\phi + \frac{v\Sigma_f - \Sigma_a}{D}\phi = 0$$

$$\Sigma_i = N \cdot \frac{\int_0^{E_c} \sigma_i(E)\phi(E)dE}{\int_0^{E_c} \phi(E)dE}$$



Step 2 : diffusion (3D)

- Precise resolution of the transport equation on limited geometry, with periodic boundaries



Step 1 : transport (2D)

Diffusion approximation : an efficient method with strong limitations

Limitation #1 – Transport calculations are performed on an infinite geometry :

- Diffusion data do not depend on the localization
- Environment is completely neglected

➤ Issues for interfaces modeling :

A strong increase of the neutron flux at the interface due to the local increase of fission cross section

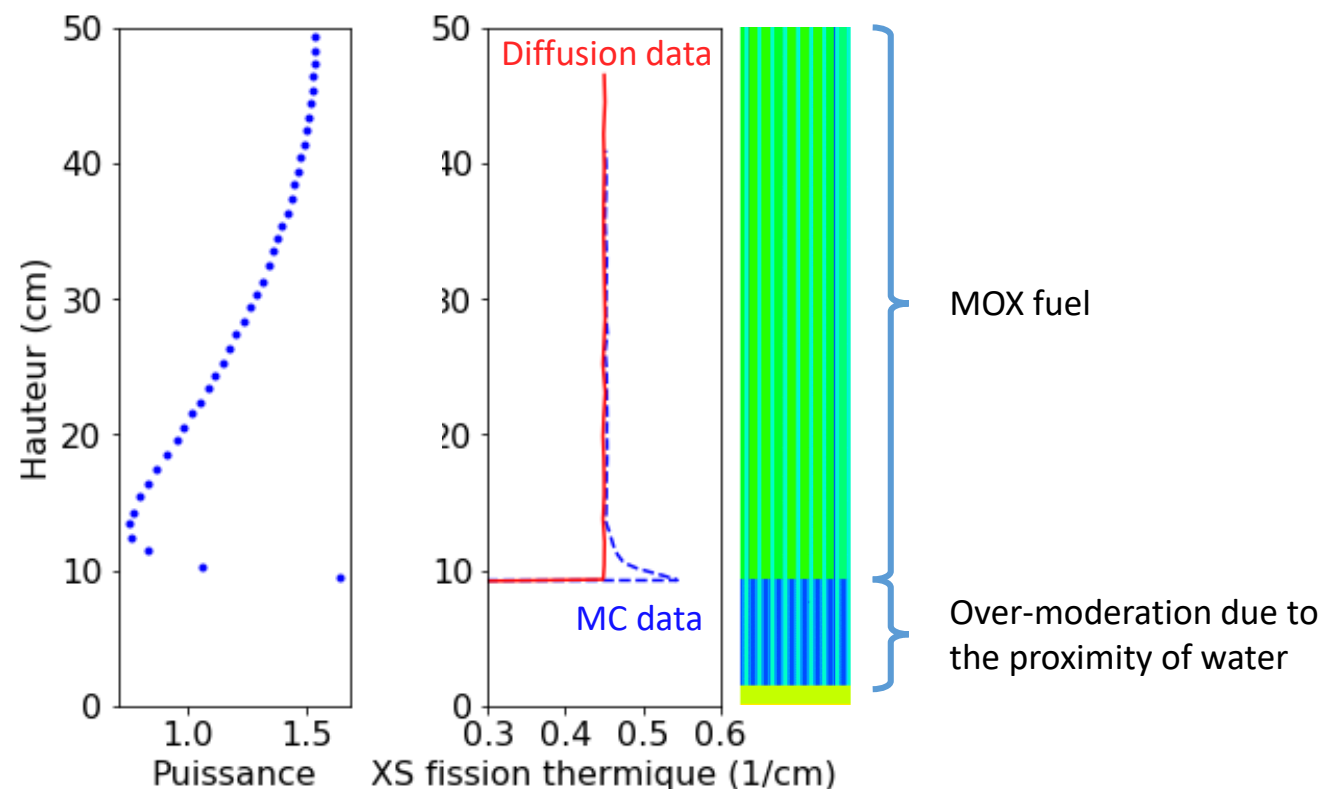
→ Badly modeled by the classical transport/diffusion scheme

➤ Improve the production/handling of diffusion data

- New variable (localization, neighbors, boron,...)
- New interpolation methods (ANN,...)

→ *NEEDS project (IN2P3/IRSN/Poly Montreal) : MADIFF*

→ *Collaboration with Framatome : Adien Rispo PhD thesis*



Limitation #2 – How to calculate diffusion data for reflectors ?

Without fissile material, the solution of transport equation is 0

- *Data in the reflector depends on the fuel composition... but the fuel behavior depends on the reflector properties*

Limitation #3 – The system is supposed to be critical

→ Use of the α –mode decomposition

- Numerical biases have to be compared to other sources of errors, specially uncertainty induced by nuclear data

Total-Monte Carlo

➤ Principle :

Creation of n different nuclear data file

TENDL



n evaluations
(for one given nucleus)

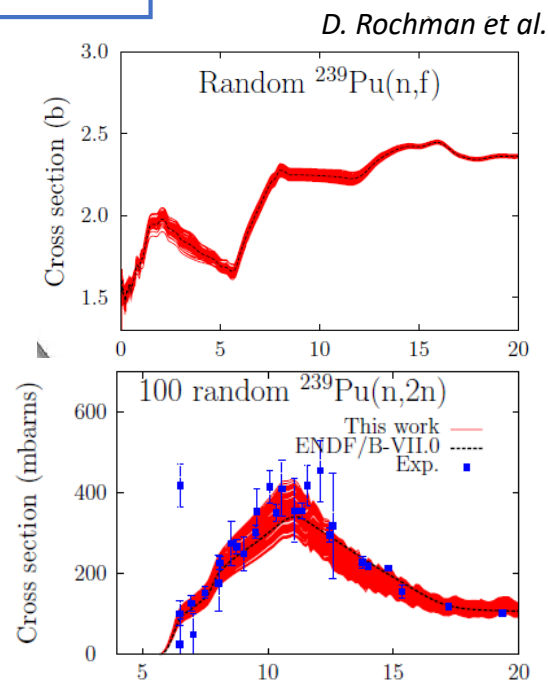


n criticality MC calculations



$\overline{k_{eff}} ; var(k_{eff})$

For each studied
nucleus



Generalized perturbation theory (GPT)

- The variance of a given observable is related to the sensitivity coefficients and the covariance matrix of the parameters

$$var(k_{eff}) = S_{\sigma}^t \cdot cov(\sigma_i, \sigma_j) \cdot S_{\sigma} \quad S_{\sigma}^k = \frac{\delta k / k}{\delta \sigma / \sigma}$$

- The adjoint equation allows sensitivity calculations

$$\frac{1}{k_{eff}} F^+ \phi^+ = M^+ \phi^+ \longrightarrow S = \frac{\langle \phi^+ | \left(\frac{\partial M}{\partial \sigma} - \lambda \frac{\partial F}{\partial \sigma} \right) \cdot \phi \rangle}{\langle \phi^+ | F \phi \rangle}$$

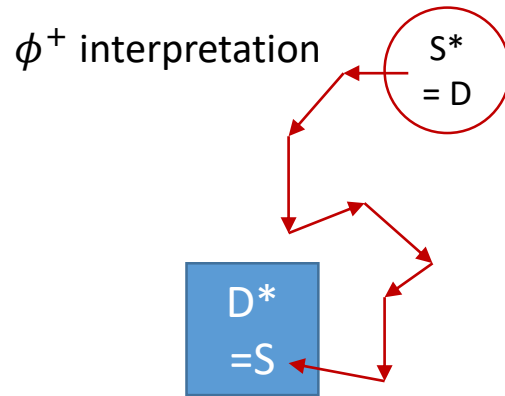
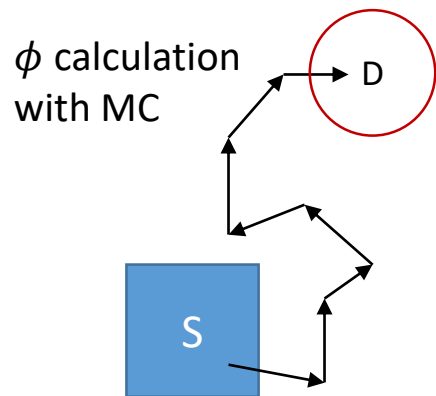
- A single direct calculation and an adjoint calculation are sufficient to estimate the uncertainties (once the covariance matrix determined)
→ Easily accessible by deterministic methods

- TMC : high computational costs + difficult physical interpretation BUT exact calculations
- GPT : more physical information and reasonable computational needs BUT approximate methods and needs of a covariance matrix
→ Explore both methods and their complementarity – production of covariance with TENDL (*Thèse Eliot Party – 2019*)

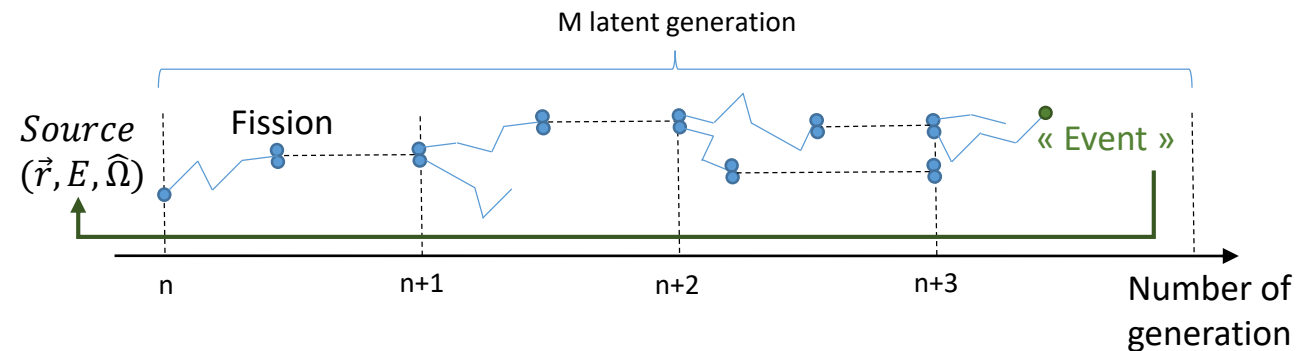
Sensitivity calculations : the revenge of Monte-Carlo methods in mid 2010s

- Physical interpretation of the adjoint flux : its relative importance related to a detection

→ « Going back in time »



- Recording successive neutron generation to track the history of fission chains
- The importance of a source neutron is then measured on every observable calculated by MC methods



- Number of *LatGen* to be adjusted regarding the observable (power distribution needs more than 100 latent generations)

Pamela Lopez et al. (2021)

- Number of LatGen directly linked to the memory needs

→ Sensibility to double differential cross-section, resonance parameters, temperature distribution,...

→ Sensitivity of modal decomposition

→ *NEEDS project (IN2P3/IRSN/CEA) : SUDEC*

- Some take home messages :
 - Two step calculation scheme is mandatory for large scale reactors
 - Homogeneous data production is a key issue :
 - MC methods may improve their relevance
 - Modal decomposition removes the assumption of stationarity
 - MC methods have shown great potentialities for sensitivity calculations

MC/Diffusion coupling calculation scheme

- Boltzmann's equation
- Coupled calculations
 - Fuel evolution
 - Reactor models for fuel cycle simulations
 - Thermal-hydraulics coupling
 - Uncertainty propagation
- Towards a common numerical framework to gather all models

Coupled calculation : fuel evolution

- Reaction rates are necessary to compute the fuel evolution described by Bateman's equation

$$\left\{ \begin{array}{l} \frac{dN_i}{dt} = -(\lambda_i + \overline{\sigma_{i,tot} \cdot \varphi}) N_i + \sum_{j \neq i} (\lambda_{j \rightarrow i} + \overline{\sigma_{j \rightarrow i} \cdot \varphi}) N_j \\ \vec{N}(t=0) = \vec{N}_0 \end{array} \right.$$

Disappearance *Production*

→ The neutron spectrum (and the reaction rates) are dependent to the fuel composition

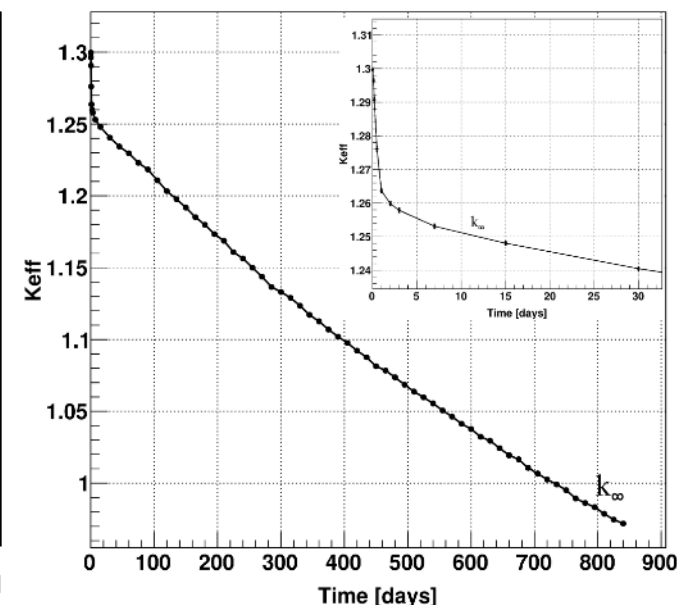
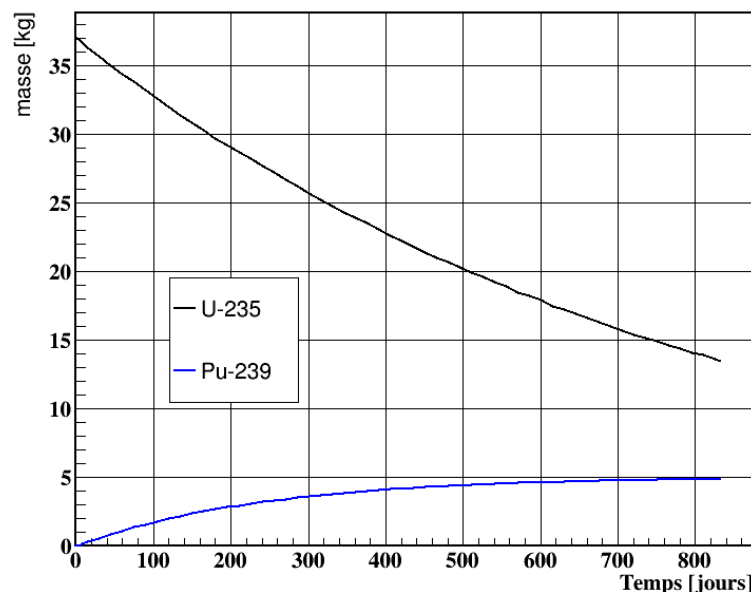
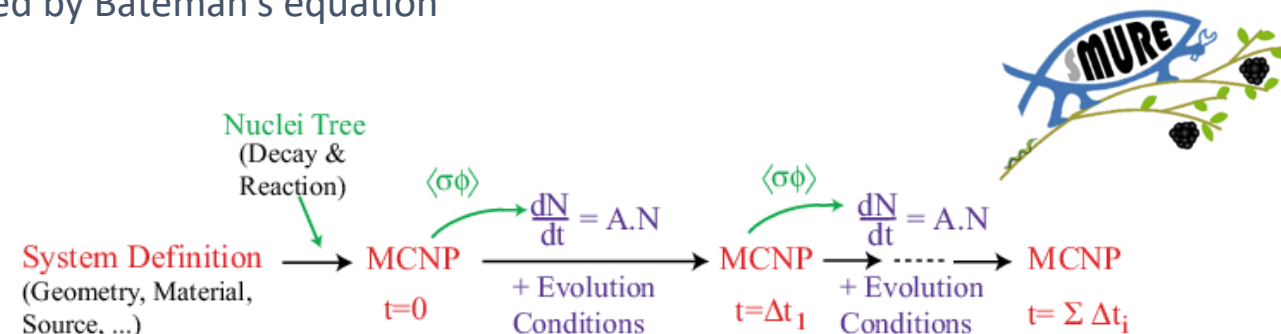
- For prospective studies, fresh fuel composition is unknown !
- Tens of SMURE calculation are needed to determine resources consumption and waste production
- To speed up calculation, use of ANN for :

$$k_{eff}(t) = f(\vec{Pu}, \%_{Pu}, t)$$

$$\sigma_i^r(t) = g(\vec{N}_0, t)$$



Principle of reactor modeling in CLASS (cf. M. Ernoult presentation)

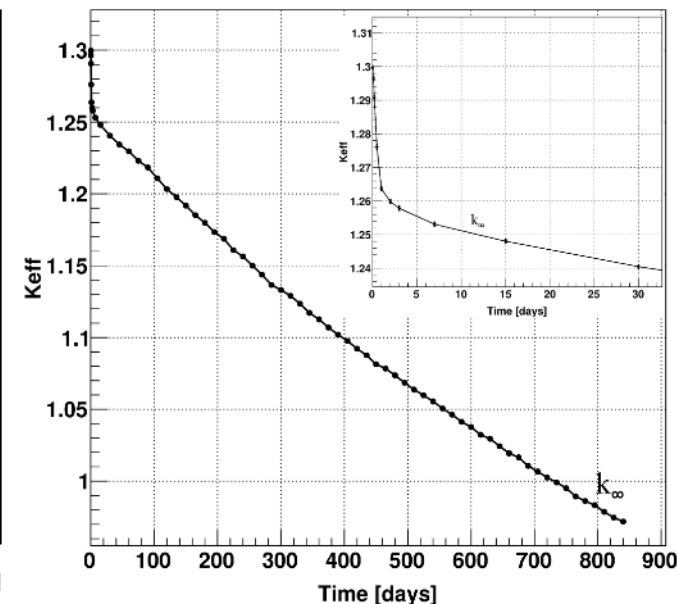
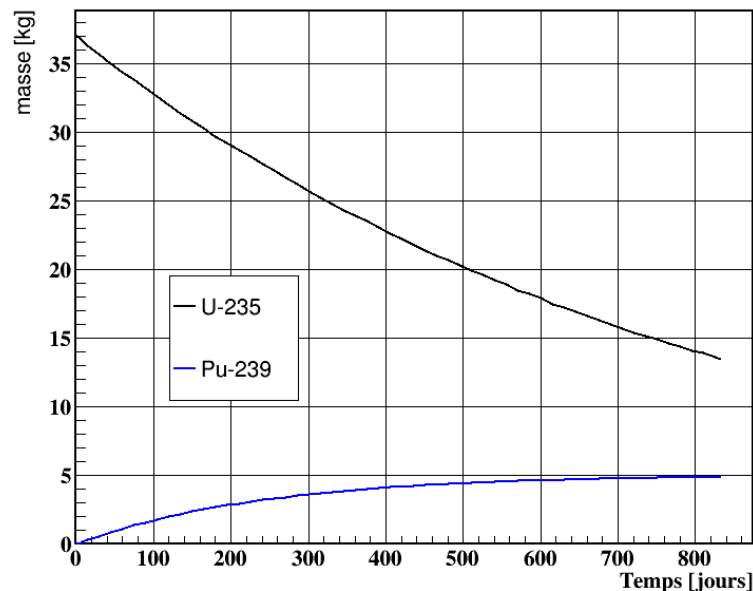
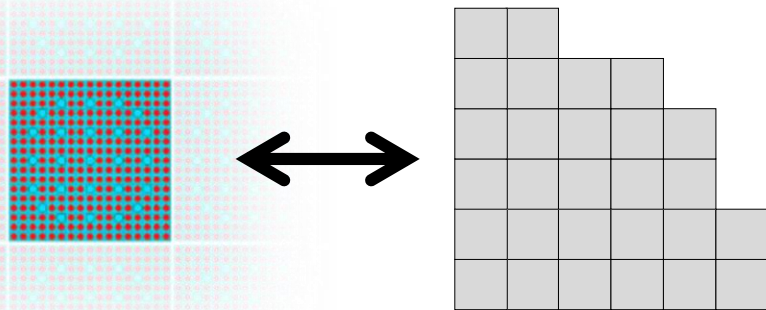


Coupled calculation : fuel evolution

- Reaction rates are necessary to compute the fuel evolution described by Bateman's equation

$$\left\{ \begin{array}{l} \frac{dN_i}{dt} = -(\lambda_i + \underbrace{\overline{\sigma_{i,tot} \cdot \phi}}_{\text{Disappearance}}) N_i + \sum_{j \neq i} (\lambda_{j \rightarrow i} + \underbrace{\overline{\sigma_{j \rightarrow i} \cdot \phi}}_{\text{Production}}) N_j \\ \vec{N}(t=0) = \vec{N}_0 \end{array} \right.$$

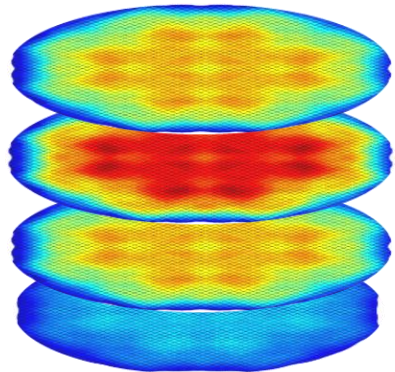
- ➔ The neutron spectrum (and the reaction rates) are dependent to the fuel composition
- ➔ Average cross section are also dependent on the localization



- ➔ Assembly calculation are not representative of full core evolutions Alice Somaini et al. (2017)
- ➔ Improvement of calculation scheme (collaboration with Polytechnique Montreal)

Fuel evolution : towards full core calculations

- Diffusion calculations mandatory for PWR
 - Use of academic DRAGON/DONJON tools from Polytechnique Montréal
- New difficulties :
 - Heterogeneous fuel
 - Loading patterns for the core
 - Reactivity follow-up (insure criticality at all time)
 - A “good” loading pattern insure a “uniform” power distribution at all time – depends on spent fuel properties
 - Goal : identify fresh fuel composition as a function of available material and
- Use of Machine Learning :
 - Sampling of possible fresh fuel composition
 - Power distribution calculation (during evolution)
 - Artificial neural network for power factor estimation as a function of many parameters



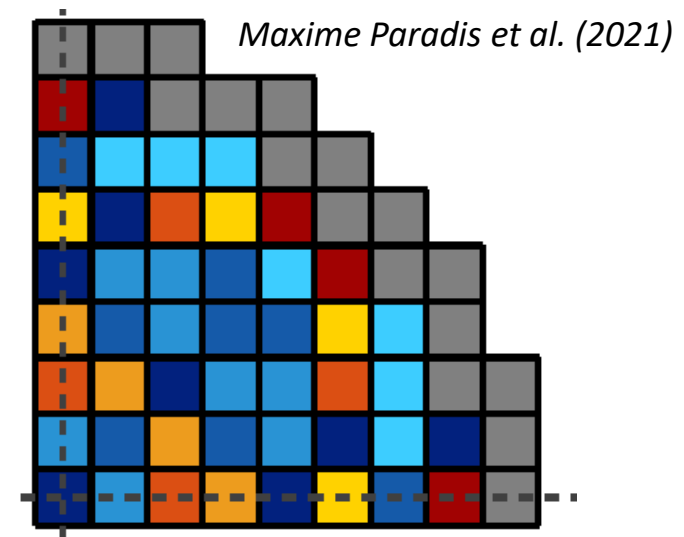
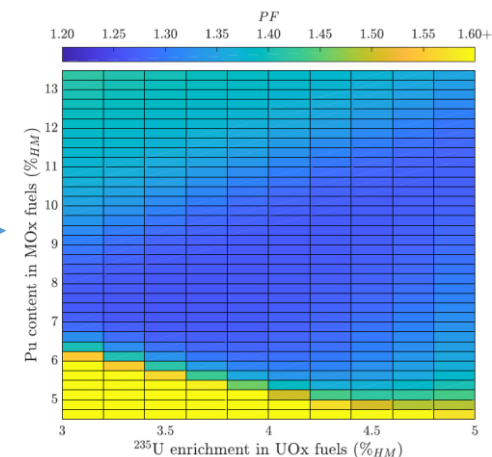
Data base construction
N simulations



$$FP = \frac{P_{max}}{P_{moy}}$$

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ANN for power factor

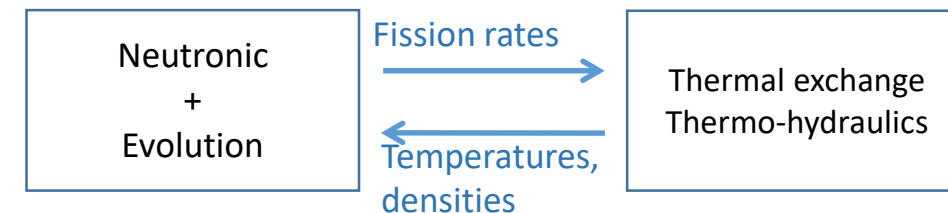


Example of a UOX/MOX loading pattern

Coupled calculations : transient studies

- Neutron reaction rates are directly dependent on the thermo-hydraulics conditions

$$\Sigma_r \psi = \sum_{\text{isotopes}} \overset{\text{Isotopic density}}{N_i} \int \overset{\text{Doppler effect on cross sections}}{\sigma_i^r(E)} \psi(E) dE$$



- Any transient study needs a coupling with thermal hydraulics

- The easiest one : the point kinetics approximation with temperature feedback coefficient → an iterative calculation scheme

$$\Phi(\vec{r}, E, t, \dots) = N(t) \cdot \phi(\vec{r}, E, \dots) \longrightarrow N(t) \sim N_0 e^{\left(1 - \frac{1}{k}\right) \frac{t}{l^*}} \longrightarrow P(t, \vec{r}) \sim N(t) \cdot \phi(\vec{r}) \longrightarrow T(t)$$

$\xleftarrow{\frac{dk}{dT}}$

- Reactor models based on point kinetics are very limited

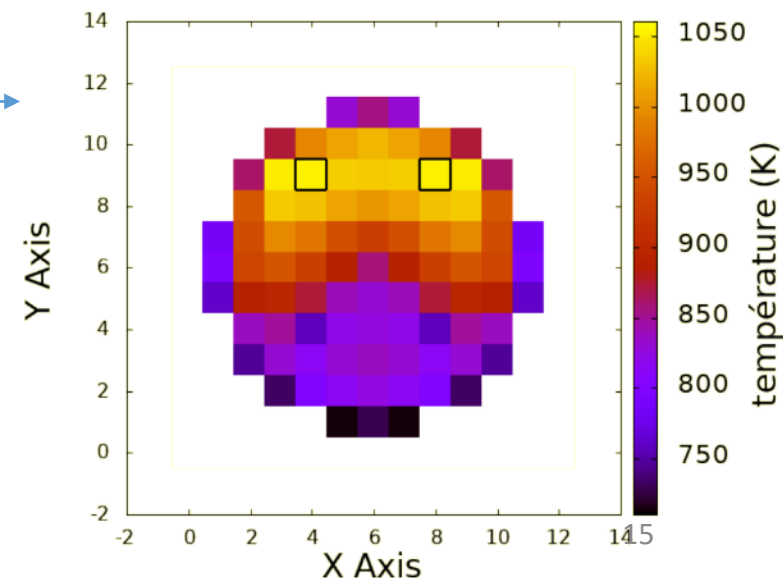
- Specially in accelerated driven system (cf. J.L. Lecouey presentation)
- Local perturbation (example : control rod ejection)

→ Nodal Drift Methods

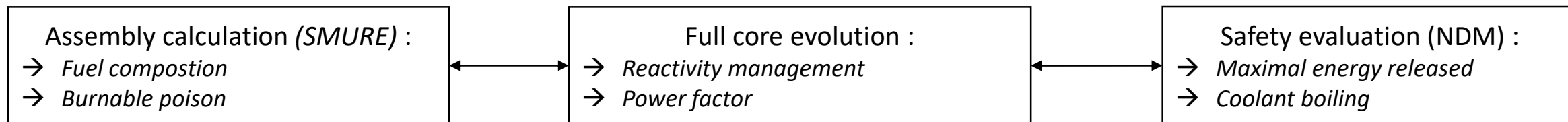
- Based on the two group diffusion with delayed neutrons

$$\begin{cases} \frac{1}{v_1} \frac{d\phi_1}{dt} = D_1 \Delta \phi_1 - \Sigma_a^1 \phi_1 - \Sigma_{1 \rightarrow 2} \phi_1 + (1 - \beta) v \Sigma_f^2 \phi_2 + \lambda p \\ \frac{1}{v_2} \frac{d\phi_2}{dt} = D_2 \Delta \phi_2 - \Sigma_a^2 \phi_2 + \Sigma_{1 \rightarrow 2} \phi_1 \\ \frac{dp}{dt} = \beta v \Sigma_f^2 \phi_2 - \lambda p \end{cases}$$

Relies on diffusion data



Transient calculations : towards a complete tool box for SMR designs



➤ Exemple : SMR in thorium cycle cooled with heavy water

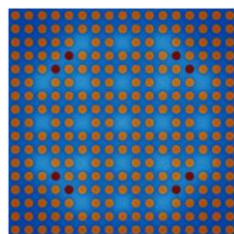
→ Under-moderation necessary for high conversion ratio

→ Reactivity monitoring by spectrum modification

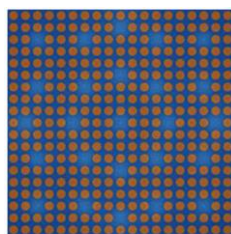
Dilution with light water

→ Transient study based on Nodal Drift Method

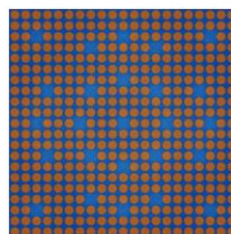
Possible stronger multiphysics coupling (cf. P. Rubiolo)



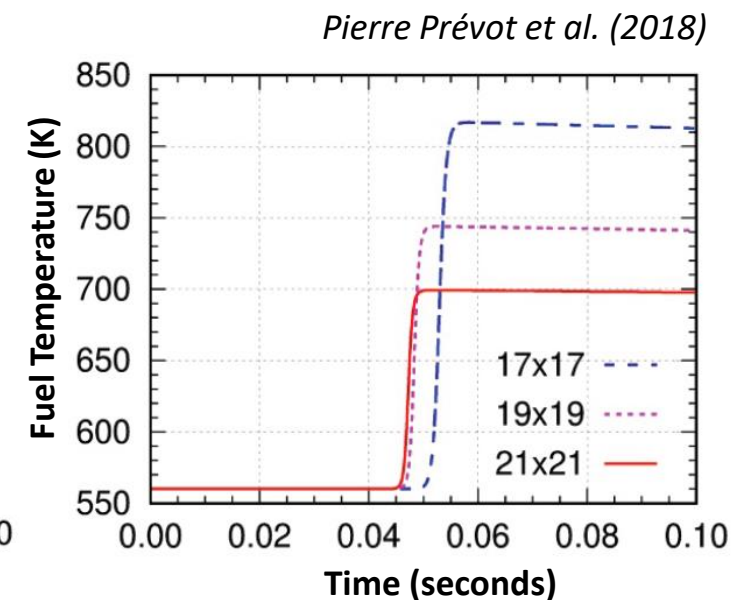
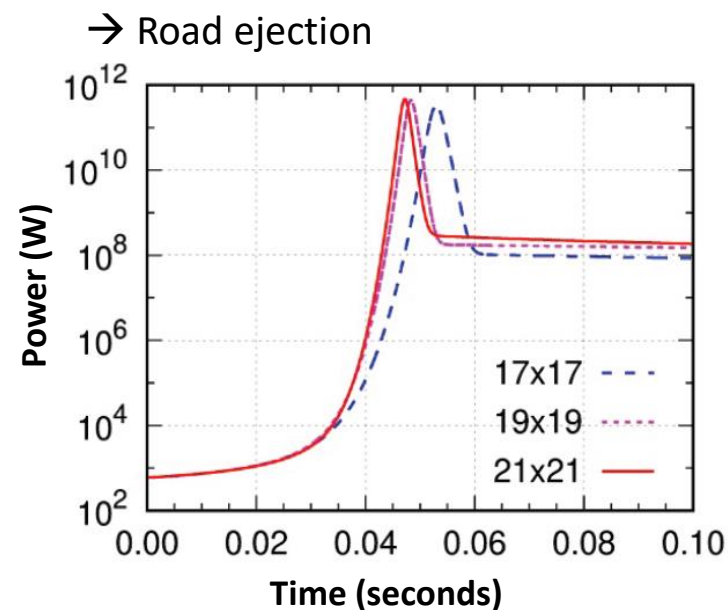
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19x19



21x21



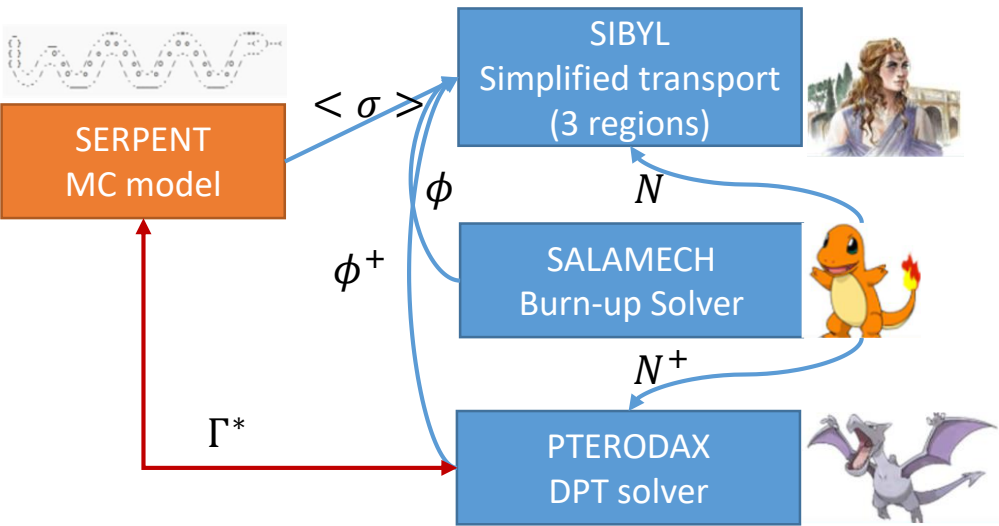
➤ The goal is not to perform safety studies, but to offer numerical to explore system potentialities

Nuclear data uncertainties for coupled calculations

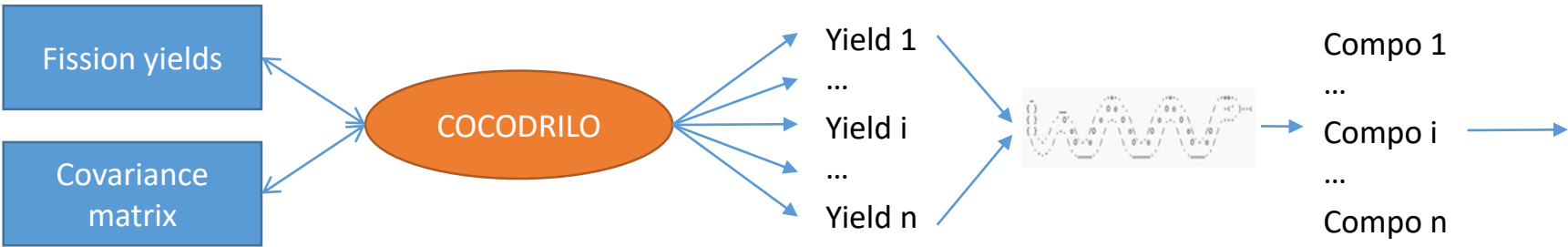
- Same methodes as for static calculations (GPT and TMC)
 - ➔ Coupling between Bateman and Boltzomann add difficulties to GPT formalism

Davide Portinari et al. (2022)

$$S_{\alpha} = \sum_i \left(\int_{t_i}^{t_{i+1}} N_i^* \frac{\partial(M_i N_i)}{\partial \alpha} dt - \langle \Gamma_i^* | \frac{\partial B_i}{\partial \alpha} \psi_i \rangle - \langle P_i^* | \frac{\partial(\sigma_i N_i)}{\partial \alpha} \psi_i \rangle \right)$$

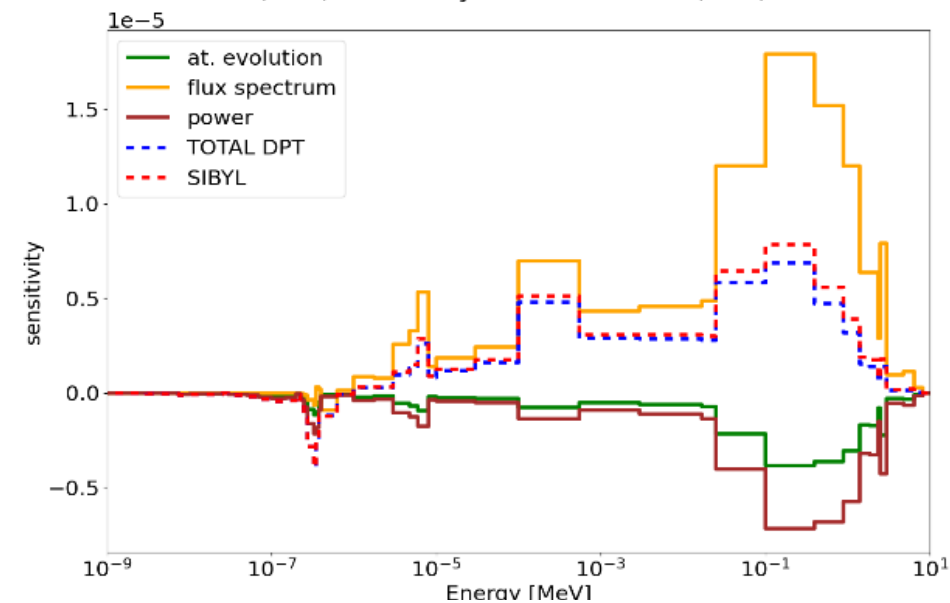


- ➔ TMC applied to depletion calculation
- ➔ COCODRILO development for fission yields and decay heat calculations

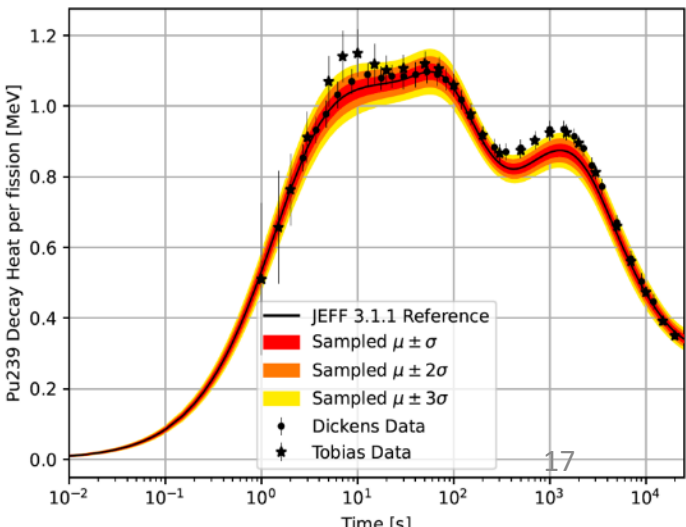


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EOL Plutonium-239 (Fuel) Sensitivity to Uranium-235 (Fuel) fission cross section



Pulse 239 Pu - Thermal neutrons - 10k Simulations



- Some take home messages :
 - Fuel assembly depletion calculation are biased compared to full core depletion calculation
 - Bias ~OK for prospective studies, not OK for precise evolution studies
 - Point kinetics not precise enough for accidental transient studies
 - Needs of spatial description of the neutron flux dynamics
 - Uncertainty propagation to depletion calculations needs simplified transport model
- *Relies on homogeneous data*
- Boltzmann's equation
- Coupled calculations
- Towards a common numerical framework to gather all models
 - Interest and challenges
 - Some key points
 - As a first step : the OSCAR project

Some huge progress in the 2010s : challenging for knowledge maintenance

- Conclusion of last IN2P3 scientific council : 3 axes to developed
 - In 2013 :
 - No fuel cycle dynamic simulators
 - Almost no transient studies
 - Beginning of GPT theory (not in evolution)
 - In 2022 : lot's of innovative methods available to address those issues
 - Sharing a same philosophy
 - Numerous software developed under different standard
- Specialization with skills developments
 - **Challenge of sharing, maintaining and archiving our know-how**
 - Numerical tools are a good option to integrate skills and knowledge
- SMURE and CLASS anchor IN2P3 as a research actor on nuclear energy (at international level)
 - Promotion of our know-how to industrial partners
- **Proposal : pooling numerical developments among a common framework**
 - Building a “model library” that can be chained for any reactor physic studies
 - Quantify each model by criteria : complexity/numerical costs/ precision
 - Code to code comparison and experimental validation

➤ **Complementary work to all current studies on different systems that have to be pursued**

A common framework to gather our scientific production and knowledge

➤ Most of reactor physic studies need homogeneous data (multi-level calculation scheme)

- Diffusion (for static and depletion calculation)
- Nodal Drift method
- Modal decomposition
- Uncertainty analysis

➤ Step 1 : offer interface with transport codes to produce those macroscopic data

➤ Most of reactor physic studies need different solvers

- Transient studies = transport + thermal-hydraulics
- Evolution = Diffusion + depletion
- ...

➤ Step 2 : define a common “form” for chaining all the models together
- *Necessity of a universal geometry description*

➤ Different model performances should be compared and validate

- MC full core calculations vs transport/diffusion approximation
- Modal decomposition vs Nodal Drift Method
- TMC vs GPT

➤ Step 3 : define a filling system to share our calculations and studies

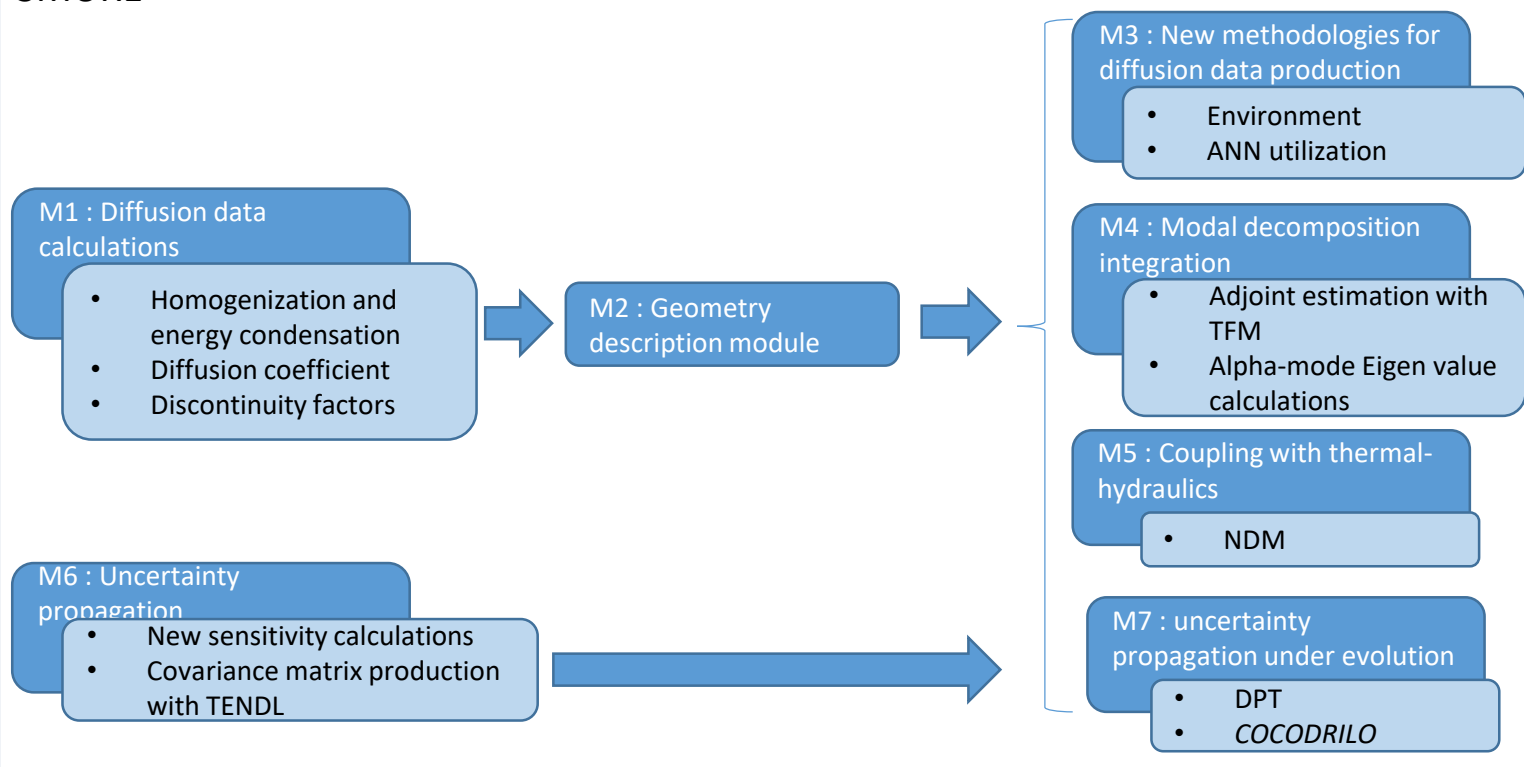
The goal is not to reproduce existent software or capabilities (like DONJON or SERPENT), but to offer a “tool box” for any kind of studies related to reactor or fuel cycle physics !

To begin with : OSCAR project

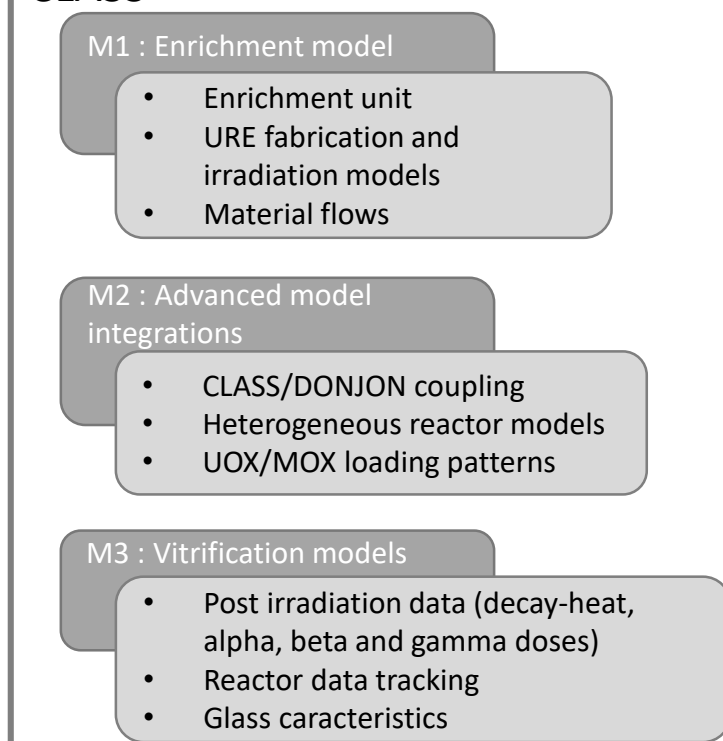
- 2022 – 2026 : OSCAR (Outils de Simulations pour les Cycles Avancés et les Réacteurs)
 - Dedicated to the integration of all recent developments in SMURE and CLASS
 - Steps and milestones defined in accordance to our human resources



SMURE



CLASS



- Those developments are performed for other scientific project (ASSURANCE, SUDEC, OKLO, SIRIUS,...)
 - Few project are only dedicated to methods and numerical developpments*



- 2022 – 2026 : OSCAR (Outils de Simulations pour les Cycles Avancés et les Réacteurs)
 - Dedicated to the integration of all recent developments in SMURE and CLASS
 - Steps and milestones defined in accordance to our human resources
- OSCAR project should prepare the future framework
 - Open access and user friendly (gather external forces)
 - Easy integration of innovative models
 - *Integration of external software ?*
- After OSCAR : possibilities will depend on the available resources
 - A numerical platform is a very ambitious and strategic project
 - It can't be done at the cost of physics projects

Numerical resources	Financial resources	Human resources
Complementarity between local and national infrastructure	Complementarity between IN2P3 and external funding (30/70)	Few Permanent staff (7 in the Oscar project) also involved in other project
CC-IN2P3 : a huge asset - Exploratory calculation - TMC - Sensitivity studies - Machine Learning	NEEDS program : much more than a financial support	11 PhD thesis defended since 2013 3 PhD thesis in progress

- Huge progress done recently in reactor modeling
 - Driven by system studies (fuel evolution, transient analysis and uncertainty calculations)
 - Development of numerous software disconnected one from each other
- **Proposal : build a common framework to gather all the developments**
 - Open access and user friendly
- 1. Strengthen our understanding of neutronics / reactor physics**
 - Explore and qualify the unitary "bricks" of reactor modeling
 - Neutronic, thermodynamic, and coupled models,...*
 - Thanks to experimental validation
 - Thanks to code to code comparison
 - Use those models for innovative system studies
- 2. Enhance our know-how and rationalize our efforts**
 - Common numerical framework
 - Promote IN2P3 as a research actor in nuclear energy