### Tracking with OFT

AGATA data analysis workshop 11-15/09/2023 Legnaro

#### Aim of tracking

Read for each event the list of deposited energies and positions of all the interactions points in AGATA

e<sub>1</sub>, x<sub>1</sub>, y<sub>1</sub>,z<sub>1</sub> e<sub>2</sub>, x<sub>2</sub>, y<sub>2</sub>,z<sub>2</sub>

e<sub>n</sub>, x<sub>n</sub>, y<sub>n</sub>, z<sub>n</sub>

Disentangle the interaction points i.e reconstruct individual photon trajectories and extract photon energies and 1<sup>st</sup> & 2<sup>nd</sup> interaction positions (for Doppler correction & polarization measurements)

#### Processes in Germanium



#### **Compton scattering**



#### What tracking does



#### What tracking does



#### What tracking does



Track order = sequence which minimizes the difference between position- and energydetermined quantities at each Compton vertex

Track deemed « complete » & accepted if the FoM of the best sequence > threshold

### Compton vertex test



$$1) \quad V_i^E = E_i - E_i^P$$

- $2) \quad V_i^e = e_i e_i^P$
- 3)  $V_i^{\cos\theta} = \cos\theta_i^E \cos\theta_i$

4)  $V_i^{\theta} = \theta_i^E - \theta_i$ 

$$E_{i} = \frac{E_{i-1}}{1 + \frac{E_{i-1}}{mc^{2}} (1 - \cos \theta_{i})}, E_{i} = E_{i-1} - e_{i}$$

$$\chi^2 = \sum_{i=1}^{N_V} \left( \frac{V_i^x}{\sigma(V_i^x)} \right)^2$$

$$\sigma^2(V_i^x) = \sum \left(\frac{\partial V_i^x}{\partial w} \Delta w\right)^2$$

(assuming normality and independence)

### Compton vertex test



$$E_{i} = \frac{E_{i-1}}{1 + \frac{E_{i-1}}{mc^{2}} (1 - \cos \theta_{i})}, E_{i} = E_{i-1} - e_{i}$$

mgt:

$$\chi^2 = \sum_{i=1}^{N_V} w_i \left(\frac{V_i^E}{E_{i-1}}\right)^2$$

1) 
$$V_i^E = E_i - E_i^P$$
  
2)  $V_i^e = e_i - e_i^P$   
3)  $V_i^{\cos\theta} = \cos\theta_i^E - \cos\theta_i$   
4)  $V_i^{\theta} = \theta_i^E - \theta_i$ 

Gretina:  $FOM = \frac{1}{N_V} \sqrt{\sum_{i=1}^{N_V} (V_i^\theta)^2}$ OFT:  $L = \prod_{i=1}^{N_V} P_i \exp^{-a \left(\frac{V_i^E}{\sigma_E}\right)^2}$ 

#### Full energy deposition or not ?

The identification is not 100% sure



#### ⇒ spectra will always contain background

⇒ Acceptance value determines the quality of the spectrum

 $\Rightarrow$  Use R = Efficiency x P/T to qualify the reconstructed spectrum

#### What limits tracking performance ?

Interaction position ≠ position of energy deposition



• Rayleigh scattering (relevant at low gamma energies and end of track)

 $\Rightarrow$  change in incident direction

#### **Electron Momentum Profile**





Biggs et al., At. Data and Nucl. Data Tab. 3 (1975) 16

#### Some more complications

From Pulse Shape Analysis:

uncertainty in position of interaction  $\delta p(e_{i_i}x_{i_j}y_{i_j}z_{i_j})$ :



position resolution



From preamplifier: energy threshold



From preprocessing: energy resolution

#### Some ambiguities....



N.J. Hammond et al., Nucl. Instr. Meth. A 547 (2005) 535–540

#### Not exactly tracking ...

1. Single interaction points:

There is not much we can do....:

- Does the interaction point satisfy photoelectric conditions (interaction depth, energy)?

- Is the interaction point sufficiently isolated from other points ?



!! With the AGATA PSA algorithm: ~20% of full absorption 1 MeV events end up in single interaction points (GEANT4 says this number should be ~10%) GRETINA PSA on the other hand yields ~1% 1 MeV single interaction points

#### Not exactly tracking ...

2. Pair production interaction points:

Do the interaction points correspond to a pair production event ?



$$e_1 = E_{\gamma} - 2 m_e c^2$$





#### **Clusterisation & Forward tracking**

0



Interaction points with an angular distance  $\leq \alpha$  between each other (link alg.) or with respect to a given point (leader alg.) constitute a CLUSTER

J. Van der Marel and B. Cederwall, Nucl. Instr. Meth. 437 (1999) 538

- Photoelectric energy deposition
   is ~ independent of incident energy
- Peaks around 100-250 keV





1. Create photoelectric interaction pool:  $e_{min} < e_i < e_{max}$ 



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distance between interaction points <  $\lambda 1$ E<sub>inc</sub> = e<sub>i</sub>+e<sub>j</sub>, E<sub>sc</sub>=e<sub>i</sub>



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#### 3. Find incident direction :

 $\cos(\theta) = 1 - m_e c^2 (1/E_{sc} - 1/E_{inc})$ 



#### 4. Find previous interaction k or source along direction

$$\begin{split} |\cos(\theta_{energy})-\cos(\theta_{geometry})| &< \text{limit} \\ \text{Prob(Compton interaction}) > \text{P}_{\text{Comp,min}} \\ \text{distance between interaction points} &< \lambda 2 \\ \text{E}_{inc}=e_i+e_j+e_k, \text{ } \text{E}_{sc}=e_i+e_j \end{split}$$

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#### Why does one use forward tracking ?

A. Lopez-Martens et al., Nucl. Instr. Meth. A 533 (2004) 454

• Geant4 => Ph. Eff. = 76%

P/T = 81%

Photon Energy = 1 MeV Multiplicity 1 and 30 Smearing - packing - energy threshold

	Ph. Eff.	P/T
Forward-tracking	<mark>61.6</mark> (33.9)	84.2 (57.7)
backtracking	40.3 (25.3)	67.0 (46.7)



Backtracking: the last points of the sequence are of low energy and close to each other  $\rightarrow$  easily packed together -> energy deposition of the "photoelectric" interaction can be much larger than 250 keV

# Performances vs position resolution & gamma multiplicity



The biggest losses are due to multiplicity (mixing points)

### Deduced position resolution @ AGATA



#### REACTION CHANNEL:<sup>48</sup>Ti(d,p)<sup>49</sup>Ti

beam	<sup>48</sup> Ti	100 MeV	
target	<sup>48</sup> Ti + <sup>2</sup> H	220 µg/cm <sup>2</sup>	
Si detector	thickness	300 µm	
	segmentation	32 rings,	
		64 sectors	
AGATA triple symmetric cluster			



### **Deduced Position resolution**



### **Deduced Position resolution**

F. Recchia et al., Nucl. Instr. Meth. A 604 (2009) 5555 simulations P.-A. Söderström et al., Nucl. Instr. Meth. A 638 (2011) 96 of the reaction 20 9.5 246 keV +18 770 keV detector 1352 keV 8.5 16 1826 keV peak (FWHM - keV) responses 2333 keV 14 3905 keV ----- Fit (8) 7.5 - Fit (10) 12 W<sub>p</sub> (mm) 10 6.5 5.5 6 **Grid Search** 4 **R. Venturelli** 4.5 2 0 3.5  $10^{2}$  $10^{3}$ E<sub>p1</sub> (keV) 12 0 position resolution (FWHM - mm)

> Is the position resolution the same in all directions? (The Doppler correction is sensitive to mostly only x & y .....)

### More recently...

Realistic uncertainties  $\sigma_{x,y,z}(e,x,y,z)$  extracted from PSA using the bootstrapping technique M. Siciliano et al., Eur. Phys. J. A (2021) 57:64



#### Effect of segment energy threshold



### Force segments to core correction



A Might not "improve" the quality of tracked spectra for cores with bad resolution

#### Background rejection



(same data used)	200 keV	500 keV	1 MeV
Centered source	P/T = 97.4% Tr. Eff = 90.5% Mgt: P/T=96.6% Tr. Eff = 95.3%	P/T=89.2% Tr. Eff. = 81.5 % Mgt: P/T=91.0% Tr. Eff = 94.5%	P/T=83.7% Tr. Eff = 80.1% Mgt: P/T=80.0% Tr. Eff = 92.7%
Off-centered source (1m from center)	P/T = 93.0% Tr. Eff = 1.6% Mgt: P/T=99.4% Tr. Eff = 57.4%	P/T=79.2% Tr. Eff. = 31.8% Mgt: P/T=77.3% Tr. Eff = 74.4%	P/T = 60.1% Tr. Eff = 40.1 % Mgt: P/T=66.6% Tr. Eff = 78.7%

#### Effect of neutrons

J. Ljungvall and J. Nyberg, Nucl. Instr. Meth. A 550 (2005) 379

#### Neutrons & Gammas

- similar signals
- similar distribution of interaction points





⇒ Large effect on P/T for low gamma multiplicities

#### ⇔Ph. Eff = -1% /n

 Can only discriminate n's and γs with good timing (can also reduce some background due to inelastic reactions (n,n'γ) with extra conditions on angles and deposited energies)

M. Senyigit et al., Nucl. Instr. Meth. A 735 (2014) 267

# Effect of encapsulation and other dead materials



Thickness of	mm
Capsule side	0.8
Cryostat side	1.5
front	3.0
back	30
Inner "ball"	10



⇒ Careful design of ancillary devices !

### Effect of simplified PSA



### Inputs to OFT

- Latest version requires 4 tracking parameters:

OftMinProbTrack	0.05	minprobtrack (default: 0.05) 🖙 FoM threshold
OftSigmaThetha	0.8	<pre>sigma_thet (default: 0.8) &lt;= Position uncertainty (cm)</pre>
OftClustRedFact	1	cluster_max_angle_reduction_factor (default: 1-> no reduction)
OftFixedAngle	0	fixed openning angle (default: 0 -> variable opening angle) 🗢 in rad

- Requires PSA hits e[i],x[i],y[i],z[i] within a given prompt coincidence time window
- Requires energies in MeV
- Requires positions in the laboratory frame in cm
- Requires knowledge of the position of the source (SourcePosition from TrackingFilter.conf)
   !! The source position is defined wrt to the center of the AGATA shell

- Does NOT require the recoil velocity or direction

### OFT – 1<sup>st</sup> steps

Calculate angles and sorts points according to increasing  $\boldsymbol{\theta}$ 

Calculate effective distances in Ge between points and between points and source

To compute proper distances, need to know positions in each detector reference frame ⇒ CrystalPositionLookUpTable





### **OFT - clusterisation**

If FixedAngle =0, compute the maximum angular separation  $\alpha_{max}$  between points in a cluster = f(n<sub>int</sub>)

$$\alpha_{\rm max} = \cos^{-1} \left( 1 - \frac{2}{\left( \left( n_{\rm int} + 2 \right) / 3 \right)^{0.9}} \right)$$

Can reduce  $\alpha_{max} = \alpha_{max} / ClusterRedFact$ 

Assign interaction points i and j to the same cluster if:

$$\cos^{-1}\left(\sin\theta_{j}\sin\theta_{i}\cos(\varphi_{j}-\varphi_{i})+\cos\theta_{i}\cos\vartheta_{j}\right) \leq \alpha$$



If FixedAngle =0, loop on  $\alpha_{min}$ (=0.15) <  $\alpha$  <  $\alpha_{max}$  and find n different clusters ( $\delta\alpha$ =0.1 rad) with total energy  $e_{clust}$ 

### OFT - tracking



If n<sub>int</sub>= 1 (mechanism 1), give the cluster
the minimal probability = MinProbTrack

If n<sub>int></sub> 1 :

If  $e_{clust}$ > 1022 keV and at least one interaction point gathers  $e_{clus}$ -1022 keV, compute the pair production probability for the cluster

Evaluate each Compton vertex of the cluster

$$E_{\gamma 1} = E_{\gamma 0} - e_{1}$$

$$E_{\gamma 1}^{P} = \frac{E_{\gamma 0}}{1 + \frac{E_{\gamma 0}}{mc^{2}}(1 - \cos \theta_{i})}$$

$$e\left[\frac{-(E_{\gamma 1} - E_{\gamma 1}^{P})^{2}}{\Delta E^{2} + \Delta P^{2}}\right]$$

$$AE = \sqrt{(n_{int} + 1)} \sqrt{\sigma_{E}}$$
average energy resolution
$$\Delta P \propto \sigma_{\theta} \sqrt{\left(\frac{\partial \cos 1}{\partial x_{0}}\right)^{2} + \left(\frac{\partial \cos \theta_{1}}{\partial y_{0}}\right)^{2} + \left(\frac{\partial \cos \theta_{1}}{\partial z_{0}}\right)^{2} + \left(\frac{\partial \cos \theta_{1}}{\partial x_{1}}\right)^{2} + \left(\frac{\partial \cos \theta_{1}}{\partial y_{1}}\right)^{2} + \left(\frac{\partial \cos \theta_{1}}{\partial z_{2}}\right)^{2} + \left$$

### OFT - tracking

1) multiply by the probability to undergo a Compton interaction at i and the probability to Compton scatter at i+1 (if i+1 is the end of the track test for photoelectric interaction):

2) multiply by the probability for ranges in Ge between i-1, i and i+1

3) skip the rest of a sequence after a bad scattering point and go to next sequence

4) Repeat for all the steps in the sequence: the total trackFOM for each sequence is the Nth square root of product of probabilities – where  $N=(n_{int}x^2)-1$ 

5) Award to the cluster the trackFOM of the best sequence or the pair production trackFOM if it is larger (and assign trackType 2 or 3 respectively)

### OFT – cluster validation

Clusters are sorted according to their figure of merit (clusters with smaller figure of merit than others and with at least one matching interaction point are flagged)

Clusters with n<sub>int</sub>>1 are accepted if trackFOM > threshold = MinProbTrack

Evaluate the FOM of the remaining unflagged single interaction clusters:

OLD METHOD

```
distance to closest interaction point > 4 cm

cross1=\sigma_{photo}(e_{clus})

cross2=\sigma_{photo}(e_{clus})+\sigma_{compt}(e_{clus})+\sigma_{pair}(e_{clus});

\lambda=range_process(cross2);

probability = sqrt(proba(\lambda, r_{qe}) \times cross1/cross2);
```

Accept cluster if trackFOM > MinProbSing (used to be an OFT parameter)

#### NEW METHOD

distance to closest interaction point > 4 cm if (proba( $\lambda$ , r<sub>ge</sub>) > f(e<sub>clus</sub>), accept single-interaction point and set trackFOM to 1.15 and trackType to 1 function f fitted from data (hence PSA dependent)

### OFT at work

AGATA + NEDA + DIAMANT @ GANIL, 2018, GANIL

 ${}^{36}$ Ar( ${}^{40}$ Ca,2p $\alpha$ ) ${}^{70}$ Se Contaminant reaction:  ${}^{36}$ Ar( ${}^{16}$ O,2p $\alpha$ ) ${}^{46}$ Ti

> MinProbTrack = 0.05 SigmaTheta= 0.8



#### Compton & Pair production clusters



SigmaTheta=0.8

### Changing parameters

SigmaTheta = 1.6 SigmaTheta = 0.8 SigmaTheta = 0.4



Optimum between gain at high energy and loss at low energy





As sigma\_theta increases, more "bad events" are accepted as Compton or pair-production clusters, reducing the number of single-interaction point clusters to be treated at the end.....and therefore reducing the efficiency at low energy and increasing the intensity of sum peaks & background at high energy

### Tracking at high-energy

Legnaro source data

Agata demonstrator (4 triple clusters) AmBe(Fe) high energy gamma-ray source source=(0,0,+5 cm) (!! the x pos. of the

source is actually lower)

might have some effect on the performance of OFT



### Tracking at high energy



### Spectra



### Tracking at high energy



### **Compton vs Pair production**

(trackType 2 vs trackType 3)



 $\star$  at 7.6 MeV, reconstruction of pair-production events contributes to ~6% of the total photopeak eff. => Compton dominates !

★ Algorithm can recognize escape and pileup peaks – very clean pair-production spectrum

### Fixed clustering angle

 $\sigma_{\theta}$ =0.4, 0.6, 0.8, 1, 1.3, 1.6, 2





1172 keV (<sup>60</sup>Co source data, 2016)

### Different behaviours.....



Fixed angle yields better performance at low energy

Variable angle is better at high energy & medium-to-high multiplicities

⇒ fine tuning of OFT parameters is needed for every experiment !

### Tracking <sup>152</sup>Eu PSA hits

In gen\_conf.py, modify the tracking parameters to see how the tracked quantities vary Run gen\_conf script and then femul (as on tuesday), sending the data to different OUT directories each time (mkdir NameofOut and then In –s NameofOut OUT)

TrackingFilter=( "ActualClass TrackingFilterOFT", # name of the used daugther class (TrackingFilterOFT or TrackingFilterMGT) "SaveDataDir \$SAVEDIR/\$MERGER". # Out/Global "EnergyGain 4", # channels/keV of the calibrated energy spectra #"ExcludeTracking", # skip the tracking part of the actor; remains only the data processing #"OftParams 0.05 0.02 0.8 100", # minprobtrack minprobsing sigma\_thet (0==default) "OftMinProbTrack 0.05", "OftSigmaThetha 0.8", "OftClustRedFact 1", "OftFixedAngle 0", #"MatParams # max value of Chi2 to accept a tracked gamma (0==default) 0 0 0", "SourcePosition # position of source with respect to the center of AGATA Position of source "DiscardEmpty 0", # to discard events that does not pass the tracking (don't discard allows to keep the events in the PSA hits)

### Tracked data

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Can Doppler correct with trackX1,trackY1 and trackzZ1 position of 1st interaction (using average beta and average beta direction or information from ancillary)

## To mock "high multiplicity" data

Change time window of hits sent to tracking filter to a much much larger value (> x1000) and play with the parameters (especially angles) to try and optimize peak intensities

EventBuilder=( "ActualClass # name of the used EventBuilder", daugther class "SaveDataDir \$SAVEDIR/\$BUILDER", # Out/Builder "Window 45", # EventNumber also possible but not working well #"TstampWindow ui64 ui64", # coincidence window 'width' or 'from to' (timestamp units) "kevIn data:psa". # key of 1st queue. "keyIn data:psa" # key of 2nd queue. 'None' to not have the surrounding frame "keyOut event:data:psa", # key of the output
frame default is event:data. 'None' to not have the surrounding frame "MinFold 1", # 2 if you want to force the coincidence between 2 AGATA